

Trigonometry

JV Practice 9/6/20

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Warm Up Problems

- (1988 AHSME #13) If $\sin(x) = 3 \cdot \cos(x)$, then what is $\sin(x) \cdot \cos(x)$?
- (AMC 2012 12A #10) A triangle has area 30, one side of length 10, and the median to that side of length 9. Let θ be the acute angle formed by that side and the median. What is $\sin \theta$?
- (C.J.) In triangle ABC , side $AB = 6$, $AC = 12$, and $\tan(A) = 2$. Compute the area of ABC .

Guided Problems

- (Law of Sines) In triangle ABC , with side lengths $BC = a$, $AC = b$, and $AB = c$, prove that

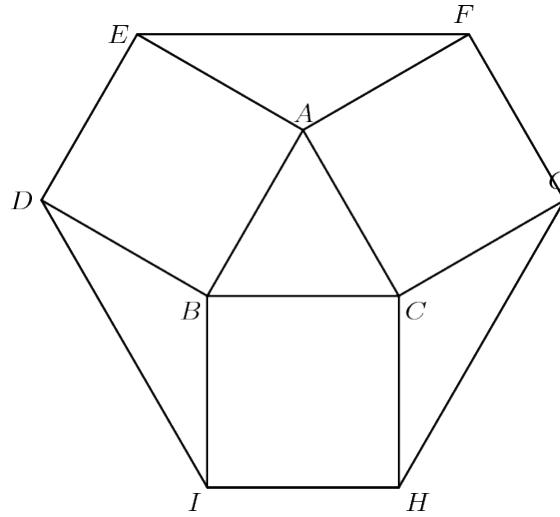
$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}.$$

Hint: use the area formula.

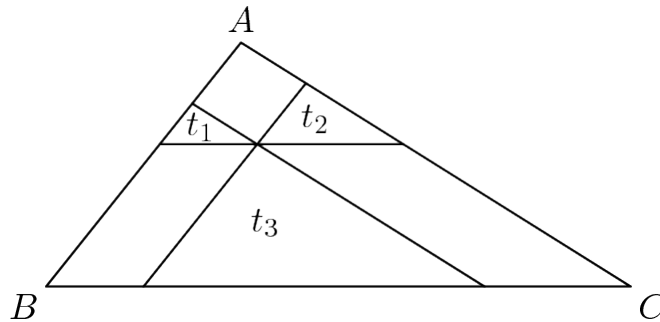
Problems

- (C.J.) Triangle ABC has $AB = 9$, $AC = 5$. Angles B and C are acute with $\tan(C) = 3 \tan(B)$. Compute the area of ABC .
- (1999 AHSME #15) Let x be a real number such that $\sec(x) - \tan(x) = 2$. What is $\sec(x) + \tan(x)$?
- (CEMC ???) In triangle PQS , point R lies on side QS such that $\angle SPR = 90^\circ$ and $\angle PRQ = 120^\circ$. If $QR = 8$ and $PR = 12$, what is the area of $\triangle QPS$?
- (2005 AMC 10B #14) Equilateral $\triangle ABC$ has side length 2, M is the midpoint of \overline{AC} , and C is the midpoint of \overline{BD} . What is the area of $\triangle CDM$?

5. (2014 AMC 10A #13) Equilateral $\triangle ABC$ has side length 1, and squares $ABDE$, $BCHI$, $CAFG$ lie outside the triangle. What is the area of hexagon $DEFGHI$?



6. (1984 AIME Problems #3) A point P is chosen in the interior of $\triangle ABC$ such that when lines are drawn through P parallel to the sides of $\triangle ABC$, the resulting smaller triangles t_1 , t_2 , and t_3 in the figure, have areas 4, 9, and 49, respectively. Find the area of $\triangle ABC$.



7. (C.J.'s crazy area problem) Prove that $ACE = BDF$ in area.

